

HSNC University Mumbai

(2023-2024)

Ordinances and Regulations

With Respect to

Choice Based Credit System (CBCS)

For the Programmes Under

The Faculty of Science and Technology

For the Course

MATHEMATICS Semester I, Semester -II

With effect from the Academic year 2023-2024

under NEP 2020

Board of Studies in Mathematics

1. Name of Chairperson

Mrs. Usha G. Hemasundar ,Head, Department of Mathematics, M Sc Mathematics Associate Professor, K. C. College Ph: 9892234921 Email id: usha.gollakota@kccollege.edu.in

Name of Co-Chairperson

Ms. Shubhada Kanchan, MSc Mathematics, Department of Mathematics and Statistics Assistant Professor, H. R. College, Ph. 9975673087 Email id: shubhadark@yahoo.co.in

- 2. Two to five teachers each having minimum five years teaching experience amongst the full-time teachers of the Departments, in the relevant subject.
 - a.) Dr. Pankit Gandhi, MSc (Mathematics), M Phil, Ph.D., LL.B., Associate Professor, K. C. College, Ph: 8169381936 Email id: pankit.gandhi@kccollege.edu.in
 - b.) Mrs. Vijayalaxmi Suvarna ,M Sc Mathematics, M.Phil ,Assistant Professor,H. R. College, Ph: 9987395783; Email id: vijayalaxmi_suvarna@rediffmail.com
 - c.) Mrs. Mrunal Hardikar ,M Sc Mathematic, Assistant Professor, K. C. College, Ph: 9653227252; Email id: mrunal.hardikar@kccollege.edu.in
 - d.) Mr. Nilesh Bhandarkar, M Sc Mathematic, Assistant Professor, K. C. College, Ph: 98200868037; Email id:nilesh.bhandarkar@kccollege.edu.in
- 3. One Professor / Associate Professor from other Universities or professor / Associate Professor from colleges managed by Parent Body; nominated by Parent Body;
 - **a.)** Dr Sushil Kulkarni , Professor, Head, School of Mathematics, Applied Statistics & Analyticas, NMIMS
- 4. External experts from Industry / Research / eminent scholar in the field relevant to the subject nominated by the Parent Body;
 - a.) Dr Ajit Kumar, Ph.D. Mathematics, Associate Professor and Head, Department of Mathematics, Institute of Chemical Technology, Mumbai
 - b.) Mrs. Jayashree Shetty, Associate Professor, KPB Hinduja College, Mumbai
 - c.) Dr. Amiya Ranjan Bhowmick, Ph.D. Applied Mathematics and Statistics; Assistant Professor, Institute of Chemical Technology, Mumbai
 - d.) Mr. Prashant Shukla, MSc statistics, Masters in Financial Management JBIMS; Chief Investment Officer, Aston Capital Advisor Pvt Ltd, Partner at HBD Consulting LLP
 - e.) Mr. Nikunj Sharma ,Zonal Head, Tata Portfolio JLL,
 - f.) Mr. Kaushal Shah, M.Com, PGDBA (Finance), Senior Manager, Treasury Reliance Power
 - g.) Mr. Ravi Vyas ,Founder S.MONK School of Actuaries
- 5. Top rankers of the Final Year Graduate and Final Year Post Graduate examination of previous year of the concerned subject as invitee members for discussions on framing or revision of syllabus of that subject or group of subjects for one year.

Ms. Gunjan Shinde, B Sc, Mathematics, Currently pursuing online Degree in data Science and Programming from IIT, Madras.

Preamble

The syllabus for major and minor courses in Mathematics are designed to lay a solid foundation for the undergraduate Mathematics student (Science Stream) in the two core aspects of Mathematics; viz the discrete and the continuous.

Discrete Mathematics involves the study of discrete objects; i.e. objects which are finite or can be enumerated by integers. It plays a foundational role in other branches of mathematics such as Number Theory, Linear Algebra, Abstract Algebra, Combinatorics, Graph Theory and Probability Theory. It also provides the mathematical foundation for many computer science courses such as data structures, automata theory, and compiler theory and computer security. The applications of Discrete Mathematics are spread across diverse areas such as Chemistry, Life Sciences, Business and Data Analysis.

While discrete means separate or distinct, continuous means without interruption or breaks. Continuous Mathematics provides excellent tools for analyzing real world phenomena that change smoothly over time. Traditional Geometry, Calculus, Real and Complex Analysis, Differential Equations, Differential Geometry, Topology and Functional Analysis are some of the branches of Mathematics which come under the banner of Continuous Mathematics. It is useful in the fields of Physics, Statistics, Economics, Finance, Artificial Intelligence, Biotechnology and Engineering.

A student who completes the minor course in Mathematics will be well equipped to understand the foundational concepts of Discrete Mathematics, Calculus and Linear Algebra which are applicable to other branches of sciences and humanities. In addition, a student who completes the major course in Mathematics will enhance their knowledge in Pure Mathematics and develop their analytical thinking ability.

Curriculum Topics along with Self-Learning Topics - to be covered, through self-learning mode along with the respective Unit. Evaluation of self-learning topics to be undertaken before the concluding lecture instructions of the respective UNIT.

The course will be conducted through the medium of lectures along with practical /lab sessions. The course assessment will include team presentations/home assignment based on self-learning topics (SLE) as well as traditional semester end written examination.

Part1: Detail Scheme Theory F.Y.B.SC. MATHEMATICS SYLLABUS (SEMESTER BASED CREDIT AND GRADING SYSTEM) IMPLEMENTED FROM THE ACADEMIC YEAR 2023-2024 under NEP as an optional major as well as minor Course

Semester – I The Scheme of Teaching and Examination

Sr.		Cho	pice Based Credit System	Subject	Remarks			
No.			·	Code				
1				MAT101B				
	Mathemat	ics(Majo	or/Minor Course)					
2	Elective	Discipl	ine Specific Elective (DSE) Course					
	Course	2.1	Interdisciplinary Specific Elective					
			(IDSE) Course					
		2.2	Dissertation/Project					
		2.3	Generic Elective (GE) Course					
3	Ability Enhancement Courses (AEC)							
	Skill Enhancement Courses (SEC)							
4	Vocation	al Cours	e-Math Section	MAT103D				

First-year Semester-I Formative and Summative Assessment Detail Scheme:

Sr. No.	Subject Code	Subject Title	Periods Per Week				Seaso	Seasonal Evaluation Scheme			Total Marks		
			Units	S. L.	L	Т	Р	Credit	S. L. E	СТ	TA	SEE	
1	MAT101B	A Foundation Course in Mathematics - I	3	20%	3	0	0	3	15	-	-	60	75
2	MAT101D	Practical based on a Foundation Course in Mathematics - I	1		0	0	1	1	-	1	-	25 (Practical Examination)	25
	Total Hours / Credit							04	Total Marks				100

Units – Topics – Teaching Hours

S.N	Subject Code		Subject Unit Title	Hours /Lect ures	Total No. of hours/lec tures	Credit	Total Marks
		I	Ordinary Differential Equations	15	45 L	3	75
1	MAT101B	II	Counting Principles	15			(60+15)
		III	Integers and Divisibility	15			
2	MAT101D		Practical sessions based on MAT101B	30	30	1	25
			TOTAL			4	100

- Lecture Duration 60 Minutes = 1 Hour
- One Credit Theory=15 Hours
- One Credit Practical=30 Hours

L: Lecture P: Practical Ct-Core Theory, Cp-Core Practical, SLE- Self-learning evaluation OBT -Open Book Test, SEE- Semester End Examination, PA-Project Assessment, AT- Attendance

Course Code: MAT101B

Title of course: A Foundation Course in Mathematics-I

Total credits: 04 (3T+1P)

Salient Features:

- In Unit 1, we focus on key concepts and methods of first order ordinary differential equations. Differential equations play a fundamental role in modern science where a differential equation is formulated to describe how a physical system changes in time. Applications of differential equations are found in Physics, Engineering, Chemistry, Biology, Economics and Finance.
- The most fundamental notion in mathematics is "Sets". Based on the concept of sets, we have a detailed study of various Counting Principles in Unit 2. The ideas presented in this unit form an integral part of Combinatorics and is used extensively in computer science.
- In Unit 3, we focus on integers and their properties. The concepts discussed here find their applications in Computer Arithmetic and Cryptography.

Learning Objectives:

- To introduce and provide the learner with fundamental concepts and applications of first order ordinary Differential Equation and Discrete Mathematics.
- 2. To develop pattern recognition and problem-solving skills of the learner.
- 3. To emphasize on understanding proofs, appreciate the language of proofs and developproof writing skills.

Course Outcomes:

- 1. Learner will be able to identify whether a differential equation is exact or non-exact, identify the most suitable method to find integrating factor for a non-exact equation, find solutions of first order differential equation and apply these ideas to formulate and solve differential equations arising naturally in basic sciences.
- 2. Learner will be able to interpret and solve problems using counting techniques based on addition and multiplication principles, pigeonhole principle and inclusion exclusion principleas well as problems based on permutations and combinations, binomial and multinomial theorems.
- 3. Learner will be able to_apply Euclidean Algorithm and back substitution to find GCD oftwo integers, apply properties of modular arithmetic to find remainders and check for divisibility. Learner will be able to construct proofs using direct argument, contradiction, taking cases or mathematical induction as required.
- 4. Learner will improve his ability in solving problems based on logical reasoning and quantitative aptitude.

Evaluation Pattern:

The course will be assessed for a total of 100 marks and will consist of:

• Summative Assessment (End Semester Theory Exam): 60 marks. Paper Pattern:

Q1: <u>Unit 1</u>: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q2: **Unit 2**: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q3: <u>Unit 3</u>: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q4: All three units: (15 marks)

Attempt any five out of seven (3 marks each)

• Formative Assessment: 40 marks.

(Self-Learning Evaluation – 15 marks (assignment or group project) and Practical Exam – 25 mark (Self-Learning Evaluation – 15 marks comprising of

- class assignment or home assignment or a case study or Group Presentation on SLE Topics (10 marks)
- Viva based on sle topics (5 marks)

Unit	Content	No. of
		Lectures
1	 Ordinary Differential Equations (ODE). Definition of a differential equation, order, degree, ordinary differential equation and partial differential equation, linear and nonlinear ODE. Methods for solving first order ordinary differential equation. Method of variable separation. Homogeneous, nonhomogeneous differential equation Exact equation ,General Solution of Exact equation of first order and first degree, Necessary and sufficient condition for M dx + N dy = 0 to be exact. Non-exact equations. 	
	 1.3 Integrating factors, Rules for finding integrating factors (without proof) for non-exact equations. 1.4 First Order linear Differential Equation, Bernoulli's equations. 1.5 Applications of first order ordinary differential equation. 	
2	 Counting Principles 2.1 Addition and Multiplication Principles, counting sets of pairs, two-way counting. 2.2 Pigeonhole principle. 2.3 Inclusion-Exclusion Principle 2.4 Permutation and combination of sets and multi-sets, circular permutations. 2.5 Binomial Theorem, Pascal's identity, Multinomial Theorem. 	15
3	 Integers and Divisibility Well Ordering Property (W.O.P) for N / W. First principle of finite Induction, Second principle of finite Induction. Divisibility in Z with properties and examples G.C.D. and L.C.M of integers. Euclidean Algorithm. Primes. Euclid's Lemma, Unique Factorization Theorem. Examples. Congruences: Definition and elementary properties. Examples. 	15

Practicals based on

Course Code: MAT101D

(15 practical sessions each of 2 lectures)

Topics	Number of
	lectures
P1 to P5: Practicals based on 1.1 to 1.5	30
P6 to P10: Practicals based on 2.1 to 2.5	
P11 to P15: Practicals based on 3.1 to 3.5.	

Self-Learning topics (Unit wise)

Unit	Topics
1	1.1 Definition of a differential equation, order, degree, ordinary differential equation and partial differential equation, linear and nonlinear ODE.
2	2.1 Addition and Multiplication Principles, counting sets of pairs, two way counting.
2	2.4, circular permutations.
2	2.5 Binomial Theorem, Pascal's identity

Online Resources

1. Basic Real Analysis' by Prof. I K Rana, IIT Mumbai

https://nptel.ac.in/courses/111/101/111101134/ lectures ,3,4,5,6

2. 'Discrete Mathematics', by Prof. Sourav from Chennai Mathematical Institute, available on Swayam-NPTEL portal

https://nptel.ac.in/courses/111/106/111106086/

3.1 First principle of finite Induction

*Subject to change if any new relevant course is available.

Reference Books:

- 1. Differential equations with applications and historical notes, by G. F. Simmons, McGraw Hill (unit1)
- 2. An introduction to ordinary differential equations E. A. Coddington,
- 3. A Foundation Course in Mathematics: Ajit Kumar, S. Kumaresan, Bhabha Kumar Sarma, 2018, Narosa Publishing House.
- 4. Discrete Mathematics: Norman L. Biggs, second Edition, Oxford University Press.
- 5. Elementary Number Theory: David Burton; Tata McGraw Hill.
- 6. Introductory Combinatorics: Richard Brualdi, John Wiley and sons.
- 7. Combinatorics-Theory and Applications: V. Krishnamurthy, Affiliated East West Press.

The Scheme of Teaching and ExaminationSemester – II

Sr.		Cho	pice Based Credit System	Subject	Remarks
No.			•	Code	
1	Mathemat	ics (Majo	or/Minor Course)	MAT102B	
2	Elective	Discipl	ine Specific Elective (DSE) Course		
	Course	2.1	Interdisciplinary Specific		
			Elective		
			(IDSE) Course		
		2.2	Dissertation/Project		
		2.3	Generic Elective (GE) Course		
3	Ability E	nhancem			
	Skill Enh	ancemer	nt Courses (SEC)		
4	Vocation	al Cours	e-Math Section	MAT104D	

First-year Semester-II Formative and Summative Assessment Detail Scheme:

Sr. No.	Subject Code	Subject Title	Periods Per Week				Seaso	Seasonal Evaluation Scheme					
			Units	S. L.	L	Т	Р	Credit	S. L. E	СТ	TA	SEE	
1	MAT102B	A Foundation Course in Mathematics - II	3	20%	3	0	0	3	15	-	1	60	75
2	MAT102D	Practical based on a Foundation Course in Mathematics - II	1		0	0	1	1	-	-	-	25 (Practical Examination)	25
	Total Hours / Credit							04	Total Marks				100

One to two lectures to be taken for CONTINUOUS self-learning Evaluation

Semester – II Units – Topics – Teaching Hours

S.N	Subject Code		Subject Unit Title	Hours /Lect ures	Total No. of hours/lec tures	Credit	Total Marks
		Ι	Relations and Functions	15	45 L	3	
1	MAT102B	II	Limits and Continuity of real-valued functions	15			75 (60+15)
		III	Differentiation of real-valued function of one variable and Applications.	15			
2	MAT102D		Practical sessions based on MAT102B	30	30	1	25
			TOTAL			4	100

- Lecture Duration 60 Minutes = 1 Hour
- One Credit Theory=15 Hours
- One Credit Practical=30 Hours

L: Lecture P: Practical T- Theory, Cp-Core Practical, SLE- Self-learning evaluation OBT - Open Book Test, SEE- Semester End Examination, PA-Project Assessment, AT- Attendance

Part2

Detail Syllabus: Semester II

Curriculum Topics along with Self-Learning topics - to be covered, through self-learning mode along with the respective Unit. Evaluation of self-learning topics to be undertaken before the concluding lecture instructions of the respective UNIT

Course Code: MAT102B

Title of course: A Foundation Course in Mathematics II

Total credits :04(3 T+ 1P)

Salient Features:

• In Unit 1, we will create a strong grounding in the topic of relations and functions. Functions are extremely significant in mathematics. We will study functions as a special type of relation and study different types of functions. The concept of relations is useful in learning Lattice theory, Boolean Algebra and Graph theory.

- In Unit 2, we focus on Continuity of functions, which is one of the core concepts in Calculus and Analysis. We will learn important properties of continuous functions on intervals of the real line and solve problems based on these properties.
- In Unit 3, we study differential Calculus which utilizes the idea of rate of change to understand the behavior of functions, such as stationary points, maxima and minima, increasing and decreasing nature of functions, concavity, convexity and point of inflection. The concepts studied here have their applications in physics, engineering, biology, economics, architecture and aviation.

Learning Objectives:

- 1. To introduce and provide the learner with fundamental concepts of Calculus and theconcepts of Relations and Functions.
- 2. To develop pattern recognition and problem-solving skills of the learner.
- 3. To develop the ability of applying concepts of Relations, Functions and Calculus.

Course Outcomes:

- Learner will be able to determine whether a relation is a function and identify its domain and range, check for bijections and compute inverse of bijective functions, demonstrate competence with equivalence relations and use this concept to find partition of sets or equivalence classes, develop proficiency with the set Zn; which is fundamental in the study of finite arithmetic.
- 2. Learner will be able to apply the ϵ - δ notion of limits to derive properties of limits, continuity and applications of continuity of real valued functions.
- 3. Learner will be able to apply the concepts of differentiability to check the increasing or decreasing nature of functions, concavity or convexity, and find maxima and minima of functions. They will be able to distinguish between various mean-value theorems, solve various limit problems using L'Hospital's rule and apply Taylor's theorem to find series expansions and approximate values of standard functions.

4. Learner will start understanding mathematical foundations in the pure mathematics.

Evaluation Pattern:

The course will be assessed for a total of 100 marks and will consist of:

Summative Assessment (End Semester Theory Exam): 60 marks.
 Paper Pattern:

Q1: <u>Unit 1</u>: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q2: **Unit 2**: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q3: <u>Unit 3</u>: (15 marks)

- A) Attempt any one out of two (7 marks each)
- B) Attempt any two out of three (4 marks each)

Q4: All three units: (15 marks)

Attempt any five out of seven (3 marks each)

• Formative Assessment: 40 marks.

(Self-Learning Evaluation – 15 marks (assignment or group project) and Practical Exam – 25 mark (Self-Learning Evaluation – 15 marks comprising of

- class assignment or home assignment or a case study or Group Presentation on SLE Topics (10 marks)
- Viva based on sle topics (5 marks)

Unit	Content	No. of
		Lectures
1	 Unit I: Relations and Functions 1.1 Definition of a Relation with examples. Function as a Relation. Domain, co domain and the range of a function. Direct and inverse images. 1.2 Injective, surjective, and bijective functions. Composite and inverse functions. 1.3 Cross product of sets. Binary Operations 1.4 Equivalence relations and partitions. 1.5 Congruence relation as an equivalence relation on Z. The set Z_n, (of residue classes modulo n) under addition and multiplication modulo n. 	15
2	 2.1 Graphs of some standard functions such as absolute value function, x², ax² + bx +c, ½, e² , logarithmic function, tan x, sin x, cosx, sin⁻¹x, x sin½, x² sin½ over suitable intervals of ℝ. 2.2 Definition of Limit of a function, Definition of Continuous functions using left-hand limit, right-hand limit. 2.3 The ε-δ definitions of limits and continuity, Evaluation of limit of simple functions using the ε-δ definition, uniqueness of limit if, exists, 2.4 Continuity of a real valued function on a set in terms of limits, Geometric Interpretation of continuity, examples, Continuity of a real valued function at end points of domain. 2.5 Boundedness theorem, Minimax Theorem, Intermediate value theorem (Statements without proof) and applications. 	15
3	 3.1Review of limit definition of differentiation of real valued function of one variable. Algebra of differentiable functions. Definition of differentiation at a point of an open interval using ε – δ, one sided derivative. 3.2 Examples of differentiable and non-differentiable functions, differentiable functions are continuous but not conversely, chain rule, Derivative of inverse functions, Higher order derivatives, Leibnitz rule, Implicit differentiation. 3.3 Local maximum and local minimum, Absolute maximum, Absolute minimum, stationary point, critical points, second derivative test, examples, graphing of functions using first and second order derivatives, convex curve, concave curve, points of inflection. 3.4 Rolle's theorem, Lagrange's and Cauchy's mean value theorems, applications and examples, Monotone increasing and decreasing function, examples. 3.5 L-Hospital rule without proof, Taylor's theorem and its applications. 	15

Practicals based on Foundation Course in Mathematics II Course Code:MAT102D

(15 practical sessions each of 2 lectures)

Topics	Number of
	lectures
P1 to P5: Practicals based on 1.1 to 1.5	30
P6 to P10: Practicals based on 2.1 to 2.5	
P11 to P15: Practicals based on 3.1 to 3.5.	

Self-Learning topics (Unit wise)

Unit	Topics
	1.1 Domain, co domain and the range of a function. Direct and inverse
1	images.
	1.2 Injective, surjective, and bijective functions. Composite and inverse
	functions
2	2.1. Definition of Limit of a function, Definition of Continuous functions using left-hand limit, right-hand limit.
3	3.1 Review of limit definition of differentiation of real valued function of one variable. Algebra of differentiable functions, one sided derivative.

.Online Resources

- 1.Basic Real Analysis by Prof Rana ,IIT Baomay, https://nptel.ac.in/courses/111/101/111101134/
- 2"Calculus of One Real variable" by Prof Joydeep Dutta, IIT Kanpur https://nptel.ac.in/courses/109/104/109104124/Week1 lecture5, week 2 lectures 1, 2, 3, 4.
- 3. 'Discrete Mathematics', by Prof. Sourav from Chennai Mathematical Institute, available on Swayam-NPTEL portal https://nptel.ac.in/courses/111/106/111106086/

Reference Books:

- 1. Introduction to Real Analysis, John Wilely & Sons, 1994 by.R. G. Bartle-D. R. Sherbert, Chapter 4,5, (unit1) Chapter6:6.1(unit 2) 6.2,6.3,6.4(unit3)
- 2. A Basic Course in Real Analysis, Ajit kumar, S. Kumaresan, CRC Press, 2014.
- 3. Thomas' Calculus by Weir, Hass, Giordano, Eleventh Edition, Pearson
- 4. Kenneth H. Rosen: Discrete Mathematics and Its Applications, McGraw Hill Edition.
- 5. Norman Biggs: Discrete Mathematics, Oxford University Press.
- 6. Bernard Kolman, Robert Busby, Sharon Ross: Discrete Mathematical Structures, Prentice-Hall India.

Part 3. Syllabus for Vocational Course

For F Y B Sc, Mathematics

Semester I

Course Title: An Introduction to Python, Sage Math, Geo Gebra Course code: MAT103D

Total credits:01

Scheme of Teaching: Total 15 practical sessions of 1 hour duration shall be conducted.

Course Objectives:

- 1. To teach students the basics of Sage Math, Geo Gebra, Python.
- 2.To train students to use CAS in mathematical problem solving for the topics taught in the Foundation Course of Mathematics-I, taught as Major/Minor Course in Semester-I

Learning Outcomes:

- 1. The students will learn basics of Python programming.
- 2 The students will know how Sage Math, Geo Gebra can be used for Mathematical problem solving.

Evaluation Pattern:

The course will be assessed for a total of 25 marks and will consist of:

- Journal consisting of output of at least 9 practicals 5 marks.
- Practical examination at end of Semester 20 marks

Note:

- 1. One practical will be of one hour each
- 2. A practical batch will according to the university norms.
- 3. Students will maintain a file/journal in which the practical questions and the output obtained in the practicals will be filed.

Detailed Syllabus

Т	Comtont	No. of
Topics	Content	Practicals
I	An Introduction to Geo Gebra: Objects, Tools and Commands, Using Sage Math for algebraic and numerical calculations	2
II	An introduction to Computing: Flowcharts, Algorithms, programs. Variables, expressions and statements, Logical operators and conditional statements in Python.	3
III	Recursions and Iterations. Strings, Lists and Tuples. An introduction to NumPy and SymPy.	4
IV	An introduction to Matplotlib, Sketching and visualizing data and functions.	2
V	Modelling a first order differential equation, solution and interpretation using Geo Gebra.	1
VI	Revision / Extra Practical.	3

List of Practicals: (Duration 1 Hour)

- P1: An Introduction to Geo Gebra: Objects, Tools and Commands.
- P2: Using Sage Math for algebraic and numerical calculations.
- P3: An introduction to Computing: Flowcharts and the way to the program.
- P4: Variables, expressions and statements in Python.
- P5: Logical operators and conditional statements in Python.
- P6: Recursions and Iterations.
- P7: Strings, Lists and Tuples.
- P8: An introduction to NumPy.
- P9: An Introduction to SymPy.
- P10: An introduction to Matplotlib I.
- P11: An introduction to Matplotlib II.
- P12: Modelling a first order differential equation, solution and interpretation using Geo Gebra.

Three more Practical sessions will be allotted for revision.

Reference Book:

- 1. Numerical Python: Scientific Computing and Data Science Applications with NumPy, SciPy and Matplotlib by Robert Johnson, Second Edition, Apress.
- 2. Mathematical Modeling Applications with Geo Gebra by Jonas Hall and Thomas Lingerfjard, Willey.
- 3. A student's guide to the study, practice, and tools of Modern Mathematics by Donald Bindner and Martin Erickson, CRC Press Taylor & Francis Group.
- 4. Geo Gebra Manual: The official manual of Geo Gebra.

Online Resources

1. Numerical Methods by Prof. Ameeya Kumar Nayak, Prof. Sanjeev Kumar by IIT Roorkee https://nptel.ac.in/courses/111/107/111107105/unit8 lecture 1, 2, 3, 4

2.Computational Mathematics with Sage Math by Dr. Ajit Kumar, Institute of Chemical Technology, Mumbai NPTEL:: Mathematics -

NOC:Computational Mathematics with SageMath

Subject to change if any new relevant course is available

Outcomes:

- 1. Student will be able to model and solve problems using CAS
- 2. Students will be able to write algorithms for some basic operations and execute those using Python.
- 3. Students will be able to apply numerical techniques for solving equations.

Online References

- 1. https://ajitmathsoft.wordpress.com/sagemath/
- 2. Computational Mathematics with Sage Math by Dr. Ajit Kumar, Institute of Chemical Technology, Mumbai NPTEL:: Mathematics NOC:Computational Mathematics with SageMath

Part4 Syllabus for Vocational Course

For F Y B Sc, Mathematics

Semester II Course Title: Numerical Techniques with Python Programming Course code: MAT104D Total credits:01

Scheme of Teaching: Total 15 practical sessions of 1 hour duration shall be conducted.

Course Objectives:

- 1 .To learn basic numerical techniques for the computation of approximate solutions of equation f(x) = 0 and of the first order of ordinary differential equation.
- 2. To train students in using Python programming for Numerical Techniques

Course Outcomes:

- 1. The students will apply various Numerical Techniques
- 2. The students will be able to execute Python programs to get approximate solutions for mathematical problems.

Evaluation Pattern:

The course will be assessed for a total of 25 marks and will consist of:

- Journal consisting of output of at least 9 practicals 5 marks.
- Practical examination at end of Semester 20 marks

Note:

- 1. One practical will be of one hour each.
- 2. A practical batch size will be according to the university norms.
- 3. Students will maintain a file/journal in which the practical questions and the output obtained in the practicals will be filed.

Detailed Syllabus

Topic	Content	No. of Practicals
I	Curve sketching, tracing and analyzing real functions for continuity and differentiability.	2
	An introduction to numerical methods, Bisection and Newton-Raphson methods, implementation using Python.	5
III	Euler's method and Runge Kutta method. Implementation using Python.	4
IV	Working with Matrices using Python.	1

V	Revision / Extra Practicals	3

List of Practicals:

- P1: Sketching and analyzing the graphs of real functions.
- P2: Curve tracing- Creating animated curves using Matplotlib.
- P3: An Introduction to Numerical Methods.
- P4: Bisection Method to solve Equation f(x)=0 using scientific calculator.
- P5: Bisection Method: Implementation using Python.
- P 6: Newton Raphson's Method to solve Equation f(x)=0 using scientific calculator.
- P 7: Newton Raphson's Method: Implementation using Python.
- P8: Euler's method: using scientific calculator.
- P9: Euler's method: Implementation using Python.
- P10: Runge-Kutta Methods: using scientific calculator.
- P11: Runge-Kutta Methods: Implementation using Python.
- P12: Working with Matrices using Python.

Three more Practical sessions will be allotted for revision.

Reference Book:

- 1. Numerical methods by E Balaguruswamy, McGraw Hill.
- 2. Numerical Python: Scientific Computing and Data Science Applications with NumPy, SciPy and Matplotlib by Robert Johnson, Second Edition, Apress.
- 3. Mathematical Modeling Applications with Geo Gebra by Jonas Hall and Thomas Lingerfjard, Willey.
- 4. A student's guide to the study, practice, and tools of Modern Mathematics by Donald Bindner and Martin Erickson, CRC Press Taylor & Francis Group.
- 5. Geo Gebra Manual: The official manual of Geo Gebra.

Online Resources

1. Numerical Methods by Prof. Ameeya Kumar Nayak, Prof. Sanjeev Kumar by IIT Roorkee https://nptel.ac.in/courses/111/107/111107105/unit lecture 1, 2, 3, 4

2.Computational Mathematics with Sage Math by Dr. Ajit Kumar, Institute of Chemical Technology, Mumbai NPTEL:: Mathematics -

NOC: Computational Mathematics with SageMath

Subject to change if any new relevant course is available